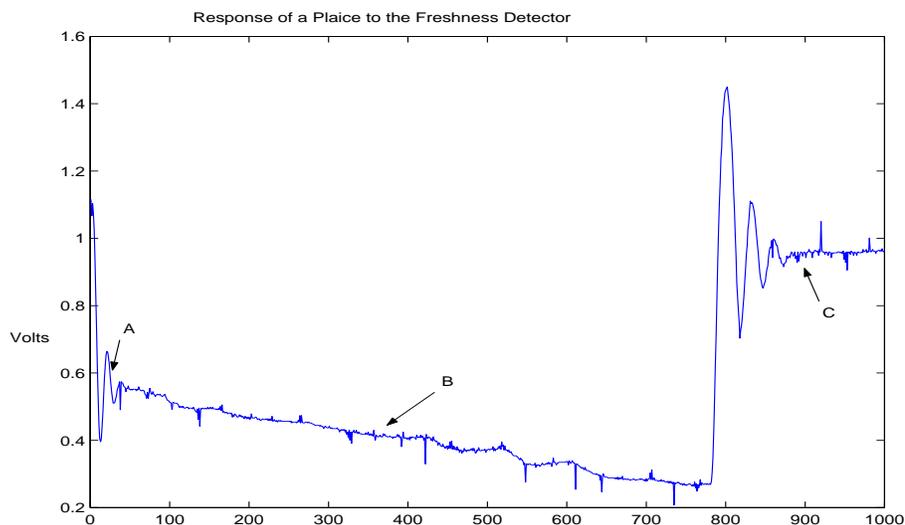


**“One fish,  
Two fish,  
Red fish,  
Blue fish”**

Modeling a Fresh Fish Detector

PIMS Modeling Group 1  
Simon Fraser University, Canada

*BURNABY, May 22, 2002*



# Presentation Outline

- Overview of model
- Digital Signal Processing: De-noising the raw data
- Analysis of distinct phases
  - Phase B
  - Phase A
  - Phase C
- Conclusions

## Overview of Model

This project models the dynamics of a device for measuring fish freshness. A needle-like probe applies a constant force to the surface of a fish and is then released. The dynamics of the fish-probe system change during the experiment, giving rise to three distinct phases:

- **Phase A:** The response resembles an oscillating decaying exponential function, which might be modeled as a mass-spring system with damping.
- **Phase B:** A linearly (or exponentially) decaying response is observed.
- **Phase C:** A second oscillating decaying exponential behavior.

The approach involved modeling the separate phases as independent processes. These were then combined to produce a working model for the entire fish-probe system.

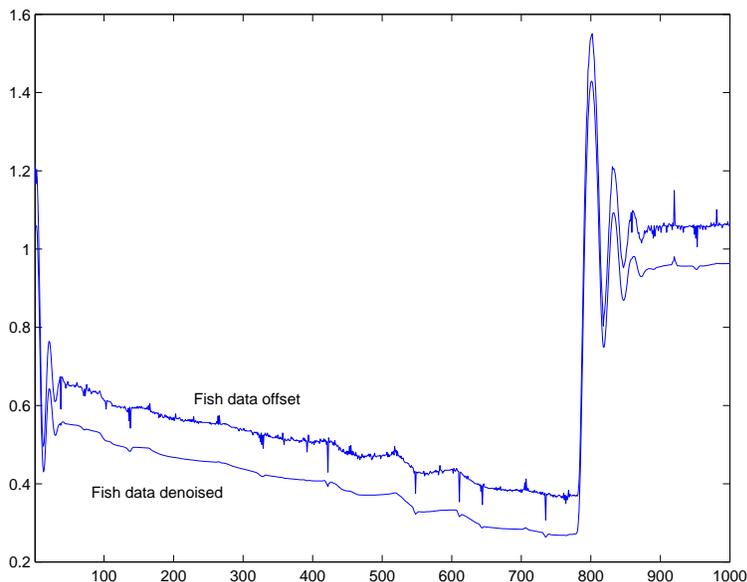
# De-noising the Raw Data

- **Why De-noising?**

1. The signal contains noise.
2. Increase the modeling accuracy by increasing the SNR.
3. Numerical computation of the velocity and acceleration of the probe.

- **De-noising methods:**

- FFT approach
- Wavelet approach ← Better!



## Phase A

We attempted to model the fish skin as a visco-elastic system described by a damped linear oscillator:

$$M\ddot{x} + \beta\dot{x} + \alpha x + Mg = 0, \quad (1)$$

where  $M = 10$  grams (mass of probe),  $g =$ gravity, and  $x = x(t)$  is the position of the probe. With constant coefficients, the solution to Equation (1) is:

$$x(t) = e^{-\delta t}[A \cos(\omega t) + B \sin(\omega t)] + D \quad (2)$$

where

$$\omega = \sqrt{\frac{\alpha}{M} - \delta^2} \quad \text{and} \quad \delta = \frac{\beta}{2M}$$

Also,  $D$  represents a vertical shift. We then fit this functional form to the data using a nonlinear least squares algorithm (Matlab). The results show that Phase A can indeed be modeled by a damped linear oscillator.

## Phase B

We model Phase B using the linear model

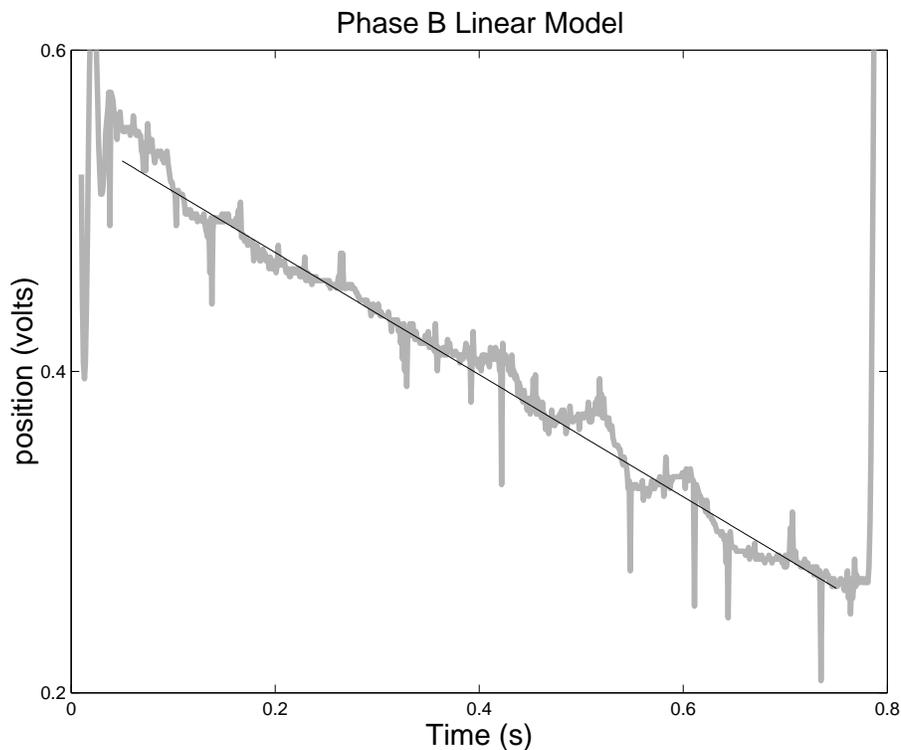
$$\alpha \dot{x} = F, \quad (3)$$

derived from *Darcy's Law* relating the *velocity* of the probe to the constant *pressure gradient* resulting from the *migration of the fluid* away from the probe.

This ODE has solution

$$x(t) = X_0 + \frac{F}{\alpha} t \quad (4)$$

and we fit the parameters  $X_0$  and  $\frac{F}{\alpha}$ .



## Phase C

Phase C also indicates damped oscillations.

- A damped linear oscillator was first implemented but did not fit the data.
- We considered a damped oscillator with nonlinear damping and restoring coefficients:

$$\alpha = \alpha_0 + \alpha_1 x + \alpha_2 x^2 \quad \text{and} \quad \beta = \beta_0 + \beta_1 \dot{x} + \beta_2 \dot{x}^2$$

- The equation was solved using Matlab, then the nonlinear least squares routine fit the resulting solution to the original fish data. The Figure reveals that a damped nonlinear oscillator cannot accurately describe the dynamics of Phase C.
- For some insight we turn to the acceleration data obtained earlier.

## Phase C

From the graph we can see:

- A section where the probe is in free fall.
- Therefore we propose a loss of contact model where the probe and fish skin separate.
- There are 3 distinct sections:
  - Section I — The force is released and the probe and skin move together in contact.
  - Section II — The probe and skin lose contact and move separately.
  - Section III — The probe and skin come back into contact and move together.

## Model the fish–probe system as an impact oscillator

- Sections I and III can be modeled with the same dynamics

- With a damped linear oscillator:

$$(M + m)\ddot{x} + \beta\dot{x} + \alpha + (M + m)g = 0 \quad (5)$$

where  $m$  = mass of fish skin in contact with the probe.

- The oscillatory behavior is interrupted by Section II.

- The solution in Section III is simply shifted in time with slight change in amplitude.

- In Section II the fish–probe system is uncoupled; probe is in free fall while the skin continues to oscillate.
- We used continuity in position and velocity to connect Sections I and II.
- The data fit well indicating an accurate model.