Outline of Math 426, Introduction to Topology

Ben Williams

First Winter Term, 2020–2021

1 Contact information

The instructor for this course is me, Ben Williams. I may be reached at tbjw@math.ubc.ca.

The course website is http://www.math.ubc.ca/~tbjw/426/index.html.

Office hours are by appointment. This is to say: email me.

2 Meeting Times

The course meets Mondays, Wednesdays and Fridays at 12pm online. A traditional lecture format will be followed.

3 Prerequisites

The formal prerequisites for this course are MATH 321, a second course in real analysis, and Math 322, a first course in group theory. At a minimum, you should be comfortable with arguments regarding continuity of functions from $\mathbb{R}^n \to \mathbb{R}^m$ and about convergence of sequences. Some homework assignments will also assume knowledge of other kinds of mathematics—please let me know if some assignment requires some knowledge you do not have.

4 Purpose

This course feeds into Math 427/527, which is a first course in algebraic topology. You should learn the basic ideas of point-set topology, and the very beginnings of algebraic topology, namely, the theory of the fundamental group and covering spaces. I will emphasize the aspects of the theory that do not overlap with functional analysis. You should also develop a high level of fluency with abstract arguments in mathematics, and learn the fundamentals of category theory.

5 Textbook

There is no required textbook for this course. Munkres' *Topology* is recommended (a paperback version may be purchased for under \$40, as is Hatcher's *Algebraic Topology* (free online) and for some light reading *Counterexamples in Topology* by Steen and Seebach (about \$15). Both lecture notes and supplementary materials will be made available.

6 Homework

Homework will be assigned throughout the course, at a rate of one assignment of three questions every week. The first assignment will be due on Friday 18 September, at 5pm. Submit homework by email, ideally in the form of a pdf compiled from LATEX.

7 Exams

There will be a take-home final exam.

8 Overall Course Grade

The overall course grade will be assigned based on homework (70%) and the final exams (30% for the final). The lowest homework grade will be dropped for each student.

9 List of Topics

The following is a list of topics that will be covered.

- 1. Topological spaces
- 2. Separation axioms
- 3. Continuous functions
- 4. Generating topologies
- 5. Induced topologies
- 6. Co-induced topologies
- 7. Closure, interior, boundary
- 8. Density
- 9. Sequence methods
- 10. Compactness

- 11. Connectedness
- 12. Path connectedness
- 13. Homotopy
- 14. The homotopy category
- 15. Homotopy groups
- 16. Paths and loops in spaces
- 17. The fundamental groupoid
- 18. Covering spaces
- 19. The relationship between the fundamental group and covering spaces
- 20. Deck transformations

- 21. The van Kampen theorem
- 22. $K(\pi, 1)$ spaces.
- 23. Topological groups and group actions
- 24. Classifying spaces from quotient constructions
- 25. Further topics as time permits

10 Policy statement

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