

ONE-SIDED AND TWO-SIDED LIMIT PROBLEMS

1. Evaluate the one-sided limits below:

a) i) $\lim_{x \rightarrow 2^-} |x - 2|$ ii) $\lim_{x \rightarrow 2^+} |x - 2|$

b) i) $\lim_{x \rightarrow -1^-} \sqrt{x^2 - 1}$ ii) Why do we not evaluate $\lim_{x \rightarrow -1^+} \sqrt{x^2 - 1}$?

$$\text{c) i) } \lim_{x \rightarrow 1^-} \sqrt[3]{\frac{x^3 - 4x^2 + 3x}{x^2 - 2x + 2}} \quad \text{ii) } \lim_{x \rightarrow 1^+} \sqrt[3]{\frac{x^3 - 4x^2 + 3x}{x^2 - 2x + 2}}$$

2. Compute the following limits:

$$\text{a) } \lim_{x \rightarrow 2} (|x - 2| + x)^5$$

$$\text{b) } \lim_{x \rightarrow 3} \frac{x^2 - 9}{x^2 - 8x + 15}$$

$$\text{c)} \lim_{x \rightarrow 0} \frac{\sqrt{x+1} - 1}{x}$$

$$\text{d)} \lim_{x \rightarrow 1} \frac{x-1}{\sqrt{2x-1}-1}$$

3. Find the values of the parameters a and b such that the function

$$f(x) = \begin{cases} (2x + a)^3, & \text{if } x < 0 \\ 5bx + 8, & \text{if } x \leq 0 < 1 \\ x^2 + 12, & \text{if } x > 1 \end{cases}$$

is continuous at all the points in its domain.