

1. We have that:

$$\int_{-1}^1 e^{u+1} du = \int_{-1}^1 e^u e^1 du = e^1 \int_{-1}^1 e^u du$$

This is why the integral evaluates to

$$e^{u+1} \Big|_{-1}^1 = e^2 - e^0 = e^2 - 1$$

Note: you can also make a substitution, letting  $r = u + 1$ , and get the same answer.

2. This question requires that you make the substitution

$$u = \frac{1}{x}, du = -\frac{1}{x^2} dx$$

With this, we now need to evaluate

$$\int_1^{1/2} -e^u du = \int_{1/2}^1 e^u du = e^u \Big|_{1/2}^1 = e^1 - e^{1/2}$$

3. Note that the distance is given by

$$\int_0^3 |v(t)| dt$$

While the displacement is given by

$$\int_0^3 v(t) dt$$

For distance, we need to find when  $v(t) < 0$  and  $v(t) > 0$ . By solving either inequality, we see that  $v(t) < 0 \iff t < \frac{5}{3}$

Therefore, the integral giving distance is

$$\int_0^3 |v(t)| dt = \int_0^{5/3} (-3t + 5) dt + \int_{5/3}^3 (3t - 5) dt$$

Evaluating this, we get

$$\left[ -\frac{3}{2}t^2 + 5t \right]_0^{5/3} + \left[ \frac{3}{2}t^2 - 5t \right]_{5/3}^3 = -\frac{3}{2} \left( \frac{5}{3} \right)^2 + 5 \frac{5}{3} + \frac{3}{2} (3)^2 - 5(3) - \frac{3}{2} \left( \frac{5}{3} \right)^2 + 5 \frac{5}{3} = \frac{41}{6}$$

The displacement is given simply by

$$\int_0^3 (3t - 5) dt = \left[ \frac{3}{2}t^2 - 5t \right]_0^3 = \frac{3}{2}(3)^2 - 5(3) = -\frac{3}{2}$$

Note: Displacement is given by  $\int |v(t)| dt$ , and not  $|\int v(t) dt|$ . If you think about what the absolute value sign does, you can see that the "reflects" negative-valued portions of the graph about  $y = 0$ , which will give you the total distance travelled, while the second gives the absolute value of the displacement.