

**Homework 4: Linear transformations; matrices. Part 1.**  
**Due Thursday February 7.**

1. Let  $V$  and  $W$  be vector spaces over a field  $F$ . Let  $A : V \rightarrow W$  be a linear transformation that has an inverse function  $B : W \rightarrow V$ . Prove that  $B$  has to be a linear transformation.
2. Problem 4.1 from Jänisch
3. Think of  $\mathbb{C}$  as a 2-dimensional vector space  $V$  over  $\mathbb{R}$ , and let  $A : V \rightarrow V$  be the linear transformation of  $V$  given by the multiplication by  $1 + 2i$  in  $\mathbb{C}$ . Write the matrix of  $A$  with respect to the standard basis of  $V$ .
4. Problems (2) and (4) from 5.4 “Test” on p. 93 of Jänisch.