

Announcements

WeBWork #7 is due tonight at 9pm

Pick up your quiz papers in the Math Learning Centre

Quiz #4 will take place here on Friday, March 4 (second half of class time)

- Covers material from Week 6 and Week 7
- As usual: no notes, no scratch paper, no phones, no calculators, etc.
- You **must** bring your student ID to class on every quiz day
- You **must** take the quiz in the section you're registered in
- You **must** stop writing when instructed to do so

Thank you for your cooperation with the exam-conditions procedures (especially staying in your seats, and not talking, until all quiz papers have been collected). It helps us a lot! and keeps the quizzes efficient.

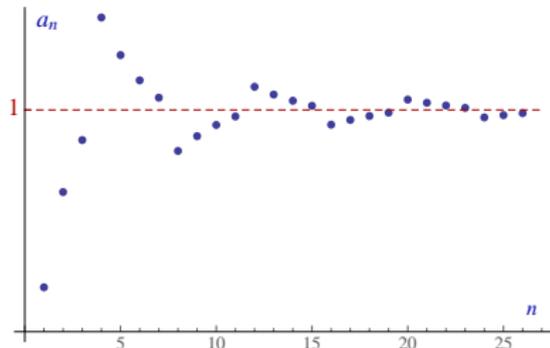
Wednesday, March 2

Clicker Questions

Clicker Question 1

Graph of a sequence

Based on the terms of the sequence you can see, does $\{a_n\}$ converge to 1 or not?



- A. no, because there's no formula for the values
- B. **yes, because the values will get as close to 1 as we like if we go far enough**
- C. no, because some values are above 1 while other values are below 1
- D. yes, because each value is closer to 1 than the previous value
- E. no, because some values are farther away from 1 than previous values

Clicker Question 2

Will this problem send you to the hospital?

Evaluate $\lim_{n \rightarrow \infty} \frac{\log n}{n^{1/9}}$.

- A. converges to 9
- B. diverges
- C. converges to $1/9$
- D. converges to 1
- E. **converges to 0**

Using l'Hôpital's Rule

It suffices to calculate $\lim_{x \rightarrow \infty} \frac{\log x}{x^{1/9}}$, which is an $\frac{\infty}{\infty}$ indeterminate form. Its limit is therefore equal to

$$\begin{aligned} \lim_{x \rightarrow \infty} \frac{(\log x)'}{(x^{1/9})'} &= \lim_{x \rightarrow \infty} \frac{1/x}{x^{-8/9}/9} \\ &= \lim_{x \rightarrow \infty} \frac{9}{x^{1/9}} = 0. \end{aligned}$$

Clicker Question 3

Applying the Squeeze Theorem

Calculate $\lim_{n \rightarrow \infty} \frac{(-1)^n + 2n + 3 \cos(4n)}{n}$.

- A. 0
- B. 1
- C. 2
- D. 3
- E. 4

Two bounding sequences

Since $(-1)^n$ is either -1 or 1 , and $3 \cos(4n)$ is always between -3 and 3 , the limit must lie between

$$\lim_{n \rightarrow \infty} \frac{2n - 4}{n} \quad \text{and} \quad \lim_{n \rightarrow \infty} \frac{2n + 4}{n},$$

both of which equal 2 .