

1 Lecture 1

References

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2 Lecture 2

References

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- [BEI92] D. C. Brydges, S. Evans, and J. Imbrie. Self-avoiding walk on a hierarchical lattice in four dimensions. *Annals of Probability*, 20:82–124, 1992. For group structure of hierarchical lattice.

3 Lecture 3

References

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- [BS] David Brydges and Gordon Slade. Self-avoiding walk. Manuscript in preparation. Theorems 1, 2 (and 3 in the next lecture) will appear here.
- [Bry07] (Defined above). See Section 6.4 for Lemma Geometric, copied from [BS].
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4 Lecture 4

Theorem 3 will appear in [BS] referenced above.

5 Lecture 5

References

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