

The mkpath package

Here are the routines defined in the file `mkpath.inc`. Roughly speaking, the entire package is concerned with building paths in $2D$.

ROUTINE: **mkgraph**
ARGUMENTS: *a f x₀ x_f N*
RETURNS: Adds a sequence of Bezier curves to the current path

The path added has N Bezier curves, along the graph of $y = f(x)$ from x_0 to x_f . The initial array contains parameters passed to the routine f . It is the *name* of the routine f which is passed as an argument (flagged by / in `PostScript`). The routine f has a fixed interface: it has two arguments, an array of parameters and a single number x , and returns an array $[f(x) f'(x)]$. The array can be empty, but it must be used in the call to `mkgraph`, and it must be removed from the stack in the routine f even if it is not used.

To draw the graph of $y = 2x^4$ from $x = -1$ to $x = 1$ we might have (among other things)

```
/quartic {  
3 dict begin  
/x exch def  
/pars exch def  
/c pars 0 def  
[  
c x mul x mul x mul x mul  
2 c mul x mul x mul x mul  
]  
end  
} def
```

```
newpath  
[2] /quartic -1 1 8 mkgraph  
stroke
```

The number N is to be chosen by experience.

ROUTINE: **mkpath**
ARGUMENTS: *a f t₀ t_f N*
RETURNS: Adds a sequence of Bezier curves to the current path

Here the routine f amounts to a parametrization of a path. It has arguments $[\dots]$ t as for `mkgraph`, and it is to return data of the form

$$[[x(t) y(t)][x'(t) y'(t)]]$$

This routine has a feature the graphing routine does not: it adds the path constructed to the current path by drawing a line from the current point if it exists to the start of the path being built. In this it acts like the command `arc` in `PostScript`.

```
/lissajous {  
4 dict begin  
/t exch 180 mul 3.1416 div def  
/pars exch def  
/m pars 0 get  
/n pars 1 get  
[  
[t m mul cos t n mul cos]  
[t m mul sin neg t n mul sin neg]
```

```
]
end
} def
```

```
newpath
[2 3] /lissajous 0 6.28 8 mkpath
stroke
```

ROUTINE: **mkpolypath**
ARGUMENTS: *a f t₀ t_f N*
RETURNS: Adds a sequence of line segments to the current path

This has exactly the same calling setup as `mkpath`, but ignores the derivative in order to build a sequence of straight segments from one position to the next. Its purpose is to help you debug your parametrization routine, to separate the derivative calculation from the position calculation.