

## Fontaine's rings and $p$ -adic $L$ -functions

This seminar will cover the study of  $p$ -adic zeta functions in the case of the cyclotomic  $\mathbb{Z}_p$ -extension of a number field  $F$ . The reading course and seminar in the summer covered the Coleman power series associated to norm compatible elements and the Coates-Wiles homomorphism. We will now switch to  $p$ -adic Hodge theory and cover Fontaine's theory of  $\phi - \Gamma$ -modules. We will then revisit the Coates-Wiles homomorphism from this set-up as well as the general machinery of  $p$ -adic  $L$ -functions. This will be independent of the earlier summer seminar as we will recall the necessary results.