Math 443 Course Syllabus 23W T1

Welcome to Math 443, Graph Theory for honours students!

Overview

From the calendar:

Introductory course in mostly non-algorithmic topics including: planarity and Kuratowski's theorem, graph colouring, graph minors, random graphs, cycles in graphs, Ramsey theory, extremal graph theory. Proofs emphasized. Intended for Honours students.

Credits: 3

Pre-reqs: A score of 68% or higher in one of <u>MATH 220</u>, <u>MATH 223</u>, <u>MATH 226</u>, <u>CPSC 121</u>. (And 6 credits of MATH numbered 300 or above.)

Grading

- 50% homework (take-home, students may work in groups)
- 20% midterm (in class, closed book, individual)
- 30% final project (scaffolded group project including assignments meant to help students learn to read math research papers, culminating in group presentations in a conference-like environment)

Textbook

A first course in graph theory, by Chartrand and Zhang

Content

- Basic definitions
- Connected graphs
- Common classes of graphs
- o Graph degree
- Walks and closed walks
- o Regular graphs
- o Degree sequences, Havel-Hakimi theorem
- Graph reconstruction conjecture and results, Kelly's theorem about disconnected graphs
- o Trees
- Minimum spanning trees and Kruskal's algorithm
- Cayley's tree formula
- Vertex- and edge connectivity
- o Blocks
- Menger's Theorem
- Eulerian circuits
- o Hamiltonicity
- o Planarity, Kuratowski's Theorem with partial proof

- Discharging
- Colouring (vertex and edge)
- Heawood's theorem with proof
- Four colour theorem, with notes on proof and history
- Embedding graphs on surfaces
- Ramsey numbers, with proofs of several results
- Time permitting: Turan's theorem, modified Ramsey numbers, random graphs, crossing number