

Course Outline
Mathematics 320 Sections 101 and 102– Real Variables I
2016W Term 1 Sept.-Dec., 2016

Prerequisite: 68% in MATH 226; or one of Math 200/217/226/253/263 and 80% in MATH 220.

Webpage for Section 101 (E. Perkins):

<http://www.math.ubc.ca/~perkins/teaching.html>

Webpage for Section 102 (I. Laba):

http://www.math.ubc.ca/~ilaba/teaching/math320_F2016/

Text: Principles of Mathematical Analysis, 3rd edition, Walter Rudin, McGraw-Hill.

Topics:

1. Number Systems (Ch. 1)

- ordered fields
- rational, real and complex numbers.
- the Archimedean property and the nonstandard reals
- supremum, infimum, completeness

2. Sequences and Series of Real Numbers (Ch. 3)

- limits of sequences, algebra of limits
- Bolzano-Weierstrass Theorem
- Cauchy sequences
- limsup, liminf
- limits of series, convergence tests, absolute and conditional convergence
- power series

3. Metric Spaces (Ch. 2)

- countable and uncountable sets; elementary set theory
- sequences in a metric space, completeness of metric spaces

- open and closed sets, closure, interior, boundary
- compact sets, Heine-Borel Theorem
- the Cantor set
- relatively open and closed sets
- connected sets

4. Continuity (Ch. 4)

- continuous functions on R and on metric spaces
- continuity and compactness, the Fundamental Theorem of Extreme Values
- continuity and connectedness, the Intermediate Value Theorem
- uniform continuity
- monotone functions

5. Differentiation; a brief review (Ch. 5)

- definitions, mean value theorem
- Taylor's theorem

Grading: Weekly or biweekly homework sets–30%
(The lowest HW score will be dropped.)

One midterm (scheduled in class for Fri. Oct. 21)–20%

Final exam–50%

The grades may be slightly scaled at the end of the course.

Other Reading

- Calculus, by M. Spivak (for axioms of the reals and sequences and series of real numbers)
- Naive Set Theory by P. Halmos (for set theory and cardinality)
- Introduction to Topology and Modern Analysis by G.F. Simmons (for more on metric spaces).