

1. (10 points) Evaluate

$$\int \frac{x^{18}}{(49-x^2)^{\frac{21}{2}}} dx$$

2. (15 points) Evaluate

$$\int \frac{x^3 - 4}{x^2 - 2x - 3} dx$$

3. (15 points) Consider the integral

$$\mathbf{I} = \int_0^1 \sqrt{1 - x^2} dx.$$

(a) Find I (use geometry). (b) Find an approximation of I using Midpoint rule and Trapezoid rule with n = 4. (c) For both Midpoint and Trapezoid rules, calculate the absolute error between the estimate and the true value.