Mathematics 602 Introduction to the Theory of Riemann Surfaces

Outline

Riemann's analysis of finite genus one dimensional complex manifolds is a mathematical gem. This course will be an introduction to these manifolds. The topics are

- Definitions and Examples
- Topology of Riemann Surfaces
- Differential Forms
- Integration Formulae
- Hodge Decomposition
- Harmonic Differentials
- Meromorphic Functions and Differentials
- Compact Riemann Surfaces
 - Bilinear Relations
 - The Riemann–Roch Theorem
 - Hyperelliptic Riemann Surfaces
 - Torelli's Theorem
- Additional topics as time permits
 - Automorphisms of Compact Riemann Surfaces
 - Theta Functions

Prerequisites

Permission of the instructors. You will need a basic knowledge of complex function theory at the level of **Complex Analysis** by Lars Ahlfors or **Functions of One Complex Variable**, Volume I, by John Conway.

Text

• H. M. Farkas and I. Kra, **Riemann Surfaces**, Springer–Verlag, 2nd Edition, 1992.

Other possible references include

- A. Beardon, Riemann Surfaces A Primer.
- C. H. Clemens, A Scrapbook of Complex Curve Theory.
- R. Miranda, Algebraic Curves and Riemann Surfaces.
- G. Springer, Introduction to Riemann Surfaces.

Instructors

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